

$$y = (x - p)^2 + q$$

+ p → shifts L
 - p → shifts R
 Math 20-1

Name: Key

Quadratic Functions and Equations

Assignment 2: Analyzing Quadratic Functions- Part 1

1. Describe how the graphs of the following functions relate to the graph of $y = x^2$

a. $y = (x + 5)^2$ + p, 5 units left horizontal translation	b. $y = x^2 - 7$ - q, 7 units ↓ vertical translation	c. $y - 8 = x^2$ $y = x^2 + 8$ + q vertical translation 8 units up
d. $y = 5 + (x - 2)^2$ vertical translation 5 units up + horizontal translation	e. $y + 7 = (x + 1)^2 - 10$ $y = (x + 1)^2 - 17$ vertical translation 17 units down, horizontal translation 1 unit left.	f. $y = (x - a)^2 - b$ vertical translation "b" units down, horizontal translation "a" units right

2. Consider the graph of the function $f(x) = (x - 2)^2 + 3$

a. Without using a graphing calculator, sketch the graph on the grid.

b. State the coordinate of the vertex.

$$(2, 3)$$

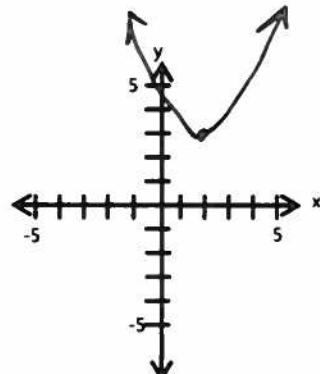
c. State maximum or minimum value of the function.

min value of 3

d. State the domain and range of the function.

domain: $\{x \in \mathbb{R}\}$

range: $\{y \mid y \geq 3, y \in \mathbb{R}\}$



$$y = (x - p)^2 + q \leftarrow \begin{matrix} \text{vertical} \\ \text{horizontal} \end{matrix}$$

3. The following transformations are applied to the graph $y = x^2$. Write the equation of the image function for each.

- a. A horizontal translation of 7 units right

$$y = (x - 7)^2$$

- b. A vertical translation of 2 units down

$$y = x^2 - 2$$

- c. A translation 3 units left and 8 units up

$$y = (x + 3)^2 + 8$$

- d. A translation c units down and d units right

$$y = (x - d)^2 - c$$

4. Write the coordinates of the image of the point $(-2, 4)$ on the graph $y = x^2$ when each of the following transformations is applied:

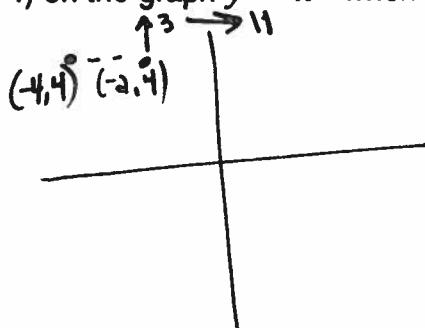
- a. A horizontal translation if 2 units to the left

$$-2 - 2, 4 \rightarrow (-4, 4)$$

- b. A translation of 3 units up and 11 units right

$$-2 + 11, 4 + 3 \rightarrow (9, 7)$$

5. Complete the following table.



Function	$y = x^2 + 5$	$y = (x + 3)^2 - 4$	$y + 9 = (x - 6)^2 + 1$ \downarrow $y = (x - 6)^2 - 8$	$y - w = (x + r)^2 + w$ \downarrow $y = (x + r)^2 + w$
Coordinates of Vertex	$(0, 5)$	$(-3, -4)$	$(6, -8)$	$(-r, w)$
Max/Min Value	min 5	min -4	min -8	min w
Equation of Axis of Symmetry	$x = 0$	$x = -3$	$x = 6$	$x = -r$
Domain	$x \in \mathbb{R}$	$x \in \mathbb{R}$	$x \in \mathbb{R}$	$x \in \mathbb{R}$
Range	$y y \geq 5, y \in \mathbb{R}$	$y y \geq -4, y \in \mathbb{R}$	$y y \geq -8, y \in \mathbb{R}$	$y y \geq w, y \in \mathbb{R}$