

Assignment

1. The graph of a function $y = f(x)$ is shown.

a) Sketch the graph of $y = \sqrt{f(x)}$ on the grid.

b) State the domain of

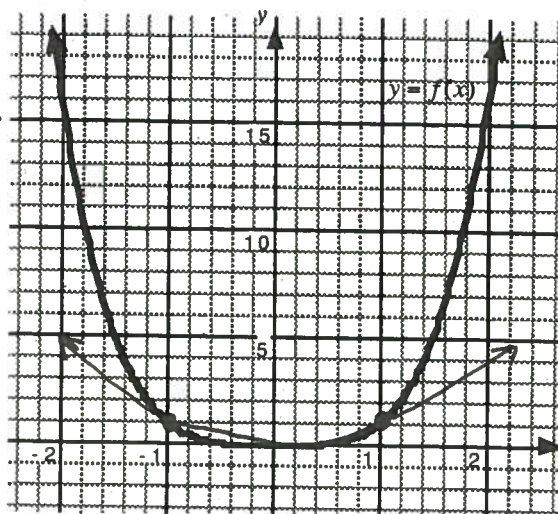
i) $y = f(x)$ $x \in \mathbb{R}$

ii) $y = \sqrt{f(x)}$ $x \in \mathbb{R}$

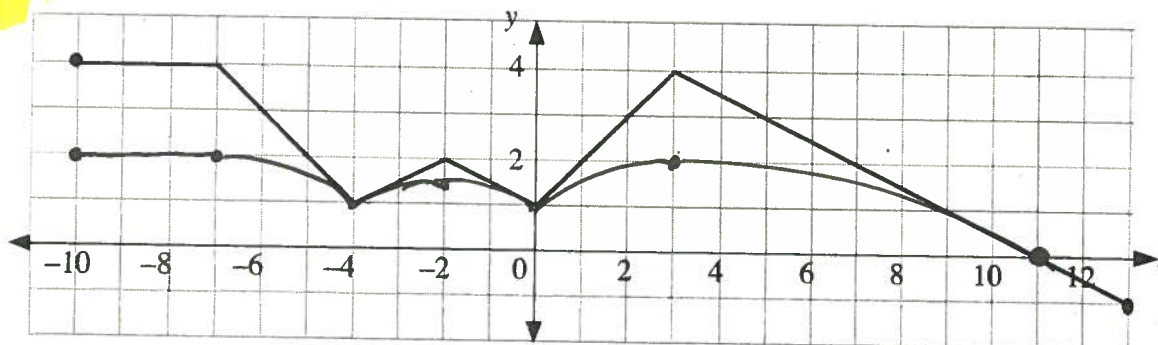
c) State the range of

i) $y = f(x)$ $y | y \geq 0, y \in \mathbb{R}$

ii) $y = \sqrt{f(x)}$ $y | y \geq 0, y \in \mathbb{R}$



2. a) The graph of a function $y = f(x)$ is shown. Sketch the graph of $y = \sqrt{f(x)}$ on the grid



b) State the domain of

i) $y = f(x)$ $x | -10 \leq x \leq 13, x \in \mathbb{R}$ ii) $y = \sqrt{f(x)}$ $x | -10 \leq x \leq 11, x \in \mathbb{R}$.

c) State the range of

i) $y = f(x)$ $y | -1 \leq y \leq 4, y \in \mathbb{R}$ ii) $y = \sqrt{f(x)}$ $y | 0 \leq y \leq 2, y \in \mathbb{R}$.

3. Given that $y = f(x)$ is a continuous function,

a) explain how you can determine the domain of $y = \sqrt{f(x)}$ from the graph of $y = f(x)$

→ the domain of $y = \sqrt{f(x)}$ is the same as that part of the domain of $y = f(x)$ for which $f(x) \geq 0$
 → If $f(x)$ is completely below x-axis, then $y = \sqrt{f(x)}$ does not exist + there is no domain

b) explain how you can determine the range of $y = \sqrt{f(x)}$ from the graph of $y = f(x)$.

→ If $f(x)$ has an x-int, the range of $y = \sqrt{f(x)}$ is from zero to the square root of the max. value of f (which could go forever)

→ If $f(x)$ is completely above the x-axis, the range is from the square root of the min. value of f to the square root of the max value of f

→ If $f(x)$ is completely below the x-axis, then $y = \sqrt{f(x)}$ does not exist + there is no range

4. The graph of a function $y = f(x)$ is shown.

a) State the domain and range of the function $y = f(x)$.

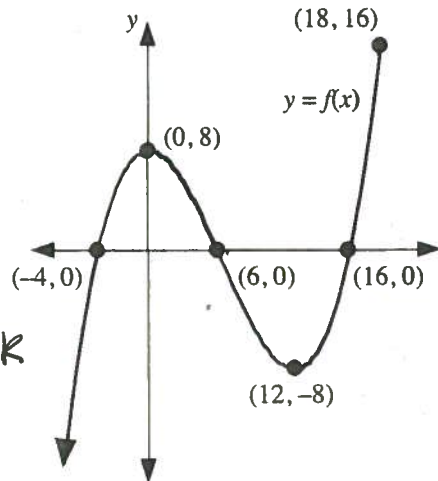
$x | x \leq 18, x \in \mathbb{R}$

$y | y \leq 18, y \in \mathbb{R}$

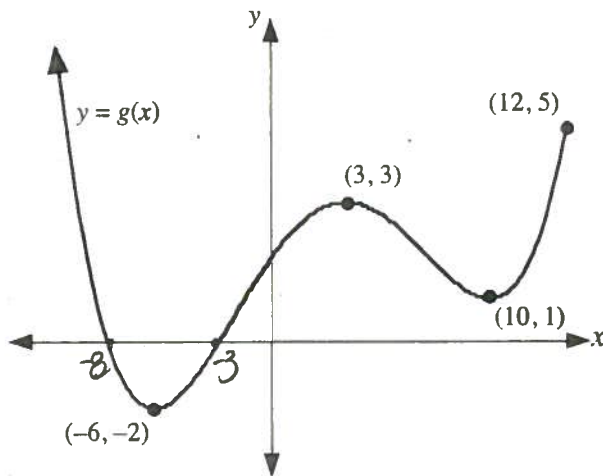
b) Without sketching the graph of $y = \sqrt{f(x)}$, determine the domain and range of the function $y = \sqrt{f(x)}$.

$x | -4 \leq x \leq 6 \text{ or } 16 \leq x \leq 18, x \in \mathbb{R}$

$y | 0 \leq y \leq 4, y \in \mathbb{R}$



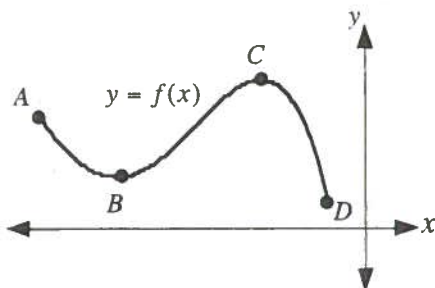
5. The zeros of the function g are -8 and -3 . The graph of $y = g(x)$ is shown below. Determine the domain and range of the function $y = \sqrt{g(x)}$.



domain of $\sqrt{g(x)}$
 $x | x \leq -8 \text{ or } -3 \leq x \leq 12, x \in \mathbb{R}$

range of $\sqrt{g(x)}$
 $y | y \geq 0, y \in \mathbb{R}$ (infinite max
 ∴ infinite range.)

6. The points $A(-12, \frac{9}{4})$, $B(-9, 1)$, $C(-4, 3)$, and $D(-2, \frac{1}{4})$ lie on the graph of $y = f(x)$ as shown. Determine the domain and range of the function $y = \sqrt{f(x)}$.

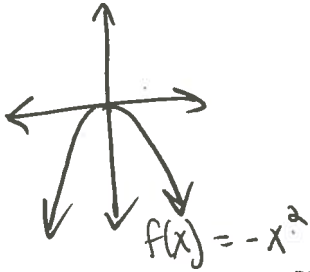


domain of $f(x)$ $x | -12 \leq x \leq -2, x \in \mathbb{R}$
 range of $f(x)$ $y | \frac{1}{4} \leq y \leq 3, y \in \mathbb{R}$

domain of $\sqrt{f(x)}$ $x | -12 \leq x \leq -2, x \in \mathbb{R}$
 range of $\sqrt{f(x)}$ $y | \frac{1}{2} \leq y \leq \sqrt{3}, y \in \mathbb{R}$

max $\sqrt{16} = 4$

7. Olivia was investigating how the graph of $y = \sqrt{f(x)}$ is connected to the graph of $y = f(x)$. She chose the example $y = f(x) = -x^2$. When she graphed $y = \sqrt{f(x)}$, she deduced from the empty screen on her graphing calculator that this graph does not exist for any values of x . Explain why Olivia's deduction is incorrect.



The graph of $y = \sqrt{-x^2}$ only exists at the point $(0,0)$. It cannot be seen on the calculator screen because it is hidden by the axes.

Use the following information to answer the next two questions.

$y = f(x)$ is a continuous function with domain $\{x \mid -4 \leq x \leq 16, x \in \mathbb{R}\}$ and range $\{y \mid -4 \leq y \leq 16, y \in \mathbb{R}\}$.

Multiple Choice

8. The domain of the function $y = \sqrt{f(x)}$ is

- A. $\{x \mid -4 \leq x \leq 16, x \in \mathbb{R}\}$
 B. $\{x \mid 0 \leq x \leq 16, x \in \mathbb{R}\}$
 C. $\{x \mid 0 \leq x \leq 4, x \in \mathbb{R}\}$
 D. unable to be determined from the given information

we do not know where $f(x) \geq 0$

9. The range of the function $y = \sqrt{f(x)}$ is

- A. $\{y \mid -4 \leq y \leq 16, y \in \mathbb{R}\}$
 B. $\{y \mid 0 \leq y \leq 16, y \in \mathbb{R}\}$
 C. $\{y \mid 0 \leq y \leq 4, y \in \mathbb{R}\}$
 D. $\{y \mid -2 \leq y \leq 4, y \in \mathbb{R}\}$

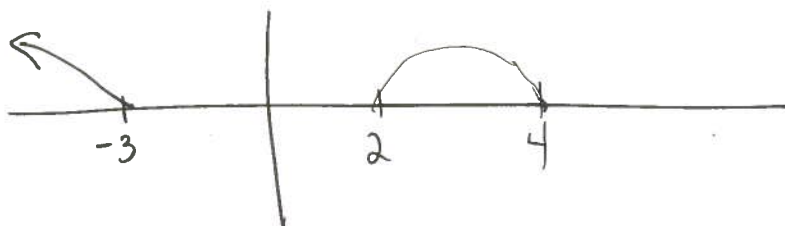
10. The range of the function $y = \sqrt{f(x)}$ is $\{y \mid y \geq 2, y \in \mathbb{R}\}$. Which one of the following statements regarding the function f must be true?

- A. The maximum value of f is 4.
 B. The function f has no zeros.
 C. The graph of $y = f(x)$ has no y -intercept.
 D. The domain of f is $x \in \mathbb{R}$.

min. value of $f = 2^2 = 4$

11. f is a continuous function with zeros -3 , 2 , and 4 . The domain of $y = \sqrt{f(x)}$ is the set of real numbers such that $x \leq -3$ or $2 \leq x \leq 4$. Which of the following values is negative?

- A. $f(-4)$ (+)
 B. $f(-3)$ (0)
 C. $f(-2)$ (-)
 D. $f(3)$ (+)



Numerical Response

12. The domain of $y = \sqrt{f(x)}$ is $x \in R$ and the range is $a \leq y \leq b$ where $y \in R$. If the minimum and maximum values of $y = f(x)$ are 12 and 36 respectively, then the product ab can be written in the form $k\sqrt{3}$, $k \in N$. The value of k is _____.

(Record your answer in the numerical response box from left to right.)

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min value of $\sqrt{f(x)} = \sqrt{12} = 2\sqrt{3}$

max value of $\sqrt{f(x)} = \sqrt{36} = 6$

$y \mid 2\sqrt{3} \leq y \leq 6$

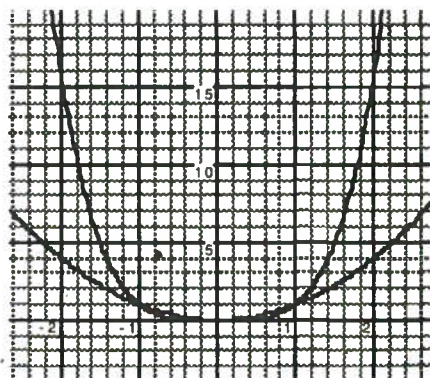
$a = 2\sqrt{3}$

$b = 6$

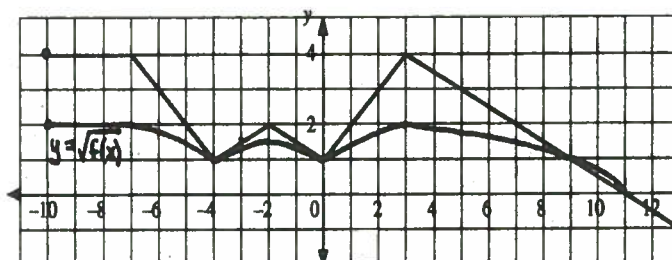
$ab = (2\sqrt{3})(6) = 12\sqrt{3}$, $k = 12$

Answer Key

1. a)



2. a)



- b) i) $\{x \mid -10 \leq x \leq 13, x \in R\}$ ii) $\{x \mid -10 \leq x \leq 11, x \in R$
 c) i) $\{y \mid -1 \leq y \leq 4, y \in R\}$ ii) $\{y \mid 0 \leq y \leq 2, y \in R\}$

- b) i) $\{x \mid x \in R\}$ ii) $\{x \mid x \in R\}$
 c) i) $\{y \mid y \geq 0, y \in R\}$ ii) $\{y \mid y \geq 0, y \in R\}$

3. a) The domain of $y = \sqrt{f(x)}$ is the same as that part of the domain of $y = f(x)$ for which $f(x) \geq 0$. If $f(x)$ is completely below the x -axis, then $y = \sqrt{f(x)}$ does not exist, and there is no domain.
 b) If $f(x)$ has an x -intercept, the range of $y = \sqrt{f(x)}$ is from zero to the square root of the maximum value of f (which could be infinite).
 If $f(x)$ is completely above the x -axis, the range of $y = \sqrt{f(x)}$ is from the square root of the minimum value of f to the square root of the maximum value of f (which could be infinite).
 If $f(x)$ is completely below the x -axis, then $y = \sqrt{f(x)}$ does not exist, and there is no range.
4. a) Domain $\{x \mid x \leq 18, x \in R\}$ Range $\{y \mid y \leq 16, y \in R\}$
 b) Domain $\{x \mid -4 \leq x \leq 6 \text{ or } 16 \leq x \leq 18, x \in R\}$, Range $\{y \mid 0 \leq y \leq 4, y \in R\}$
5. Domain $\{x \mid x \leq -8 \text{ or } -3 \leq x \leq 12, x \in R\}$, Range $\{y \mid y \geq 0, y \in R\}$
6. Domain $\{x \mid -12 \leq x \leq -2, x \in R\}$ Range $\{y \mid \frac{1}{2} \leq y \leq \sqrt{3}, y \in R\}$
7. The graph of $y = -x^2$ is a parabola with a maximum point at $(0, 0)$. The graph of $y = \sqrt{-x^2}$ will not exist when $-x^2$ is less than zero, but will exist when $x = 0$. The point $(0, 0)$ is therefore the only point the graph of $y = \sqrt{f(x)}$. It cannot be seen on the calculator screen because it is hidden by the axes. By turning the axes off on the calculator, the point $(0, 0)$ can be seen.

8. D 9. C 10. B 11. C 12.

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| 1 | 2 | | |
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